

ELIZADE UNIVERSITY, ILARA-MOKIN, ONDO STATE FACULTY OF ENGINEERING DEPARTMENT OF ELECTRICAL AND COMPUTER ENGINEERING

SEMESTER II EXAMINATION, 2016/2017 ACADEMIC SESSION

COURSE TITLE: ENGINEERING MATHEMATICS IV – 3 UNITS

COURSE CODE: GNE 316

EXAMINATION DATE: 25th JULY 2017

COURSE LECTURER: Dr. D. O. Akinyele

HOD's SIGNATURE

TIME ALLOWED: 3 HRS

INSTRUCTIONS:

- 1. ATTEMPT ANY FIVE QUESTIONS OF YOUR CHOICE
- 2. SEVERE PENALTIES APPLY FOR MISCONDUCT, CHEATING, POSSESSION OF UNAUTHORIZED MATERIALS DURING EXAM.
- 3. YOU ARE <u>NOT</u> ALLOWED TO BORROW CALCULATORS AND ANY OTHER WRITING MATERIALS DURING THE EXAMINATION.
- 4. STATE CLEARLY THE COMBINED STOPPING CONDITIONS USED IN YOUR SOLUTIONS

Question #1

(a) Draw the graph of a periodic function defined by:

$$f(x) = \begin{cases} 5, & 0 < x < 5\\ 0, & 5 < x < 7 \end{cases}$$

$$f(x+7) = f(x)$$
(2 marks)

(b) With appropriate mathematical expressions, state the condition for two functions to be orthogonal. (2 marks)

(c) Test if the following functions are orthogonal:

(i)
$$f(x) = \cos mx$$
 and $g(x) = \cos nx$ (4 marks)

(ii) $f(x) = \cos mx$ and $g(x) = \sin nx$ (4 marks)

Question #2

Let f(x) be a function of period 2π such that: f(x) = x is in the range $-\pi < x < \pi$. (a) Sketch a graph of f(x) in the interval $-3\pi < x < 3\pi$ (1 mark)

(b) Show that the Fourier series for f(x) in the range $-\pi < x < \pi$ is given by:

$$2\left(\sin x - \frac{1}{2}\sin 2x + \frac{1}{3}\sin 3x -\right)$$
 (9 marks)

(c) By giving an appropriate value to *x*, show that:

$$\frac{\pi}{4} = 1 - \frac{1}{3} + \frac{1}{5} - \frac{1}{7} + \dots$$
(2 marks)

Question #3

Determine the power series solution of the ordinary differential equation:

$$\frac{d^2y}{dx^2} + 2x\frac{dy}{dx} + y = 0$$

using the Leibnitz-Maclaurin method, given that at x = 0, y = 1 and $\frac{dy}{dx} = 2$ (12 marks)

Question #4

(a) Find the 6th derivative of the following:

(i)
$$y = \cosh 2x$$
 (2 marks)

(ii)
$$y = 2ln3\Phi$$
 (2 marks)

(b) Determine the power series solution of the Legendre equation:

$$(1-x^2)y''-2xy'+k(k+1)y=0,$$

when (i) k = 0 (ii) k = 2, up to and including the term in x^5 . (8 marks)

Question #5

(a) Find the power series solution of the Bessel function:

$$x^{2}y'' + xy' + (x^{2} - v^{2})y = 0,$$

in terms of the Bessel function $J_3(x)$. Give the answer up to and including the term in (4 marks) x^4 .

(b) Evaluate the Bessel functions:

(i)
$$J_0(x)$$
 (5.5 marks)
(2.5 marks) (2.5 marks)

(ii) $J_1(x)$, correct to 3 decimal places.

Question #6

(a) Determine the dot and cross products of the two vectors:

(6 marks) A = 2i - 3j + 4k and B = i + 2j + 5k. (b) If $\Phi = x^2 y z^3 + x y^2 z^2$, determine grad Φ at the point (1, 3, 2). (4 marks)

(i) State the condition for a vector to be solenoidal. (0.5 mark) (c) (ii) Determine **div** A of the vector $A = 2x^2yi - 2(xy^2 + y^3z)j + 3y^2z^2k$

(1.5 marks)

Question #7

(a) If = $(y^4 - x^2z^2)i + (x^2 + y^2)j - x^2yzk$, find **curl** *B* at the point (1, 3, -2).

(5 marks)

(b) Evaluate the line integral of the point V along a curve having parametric equations x = 3u; $= 2u^2$; $z = u^3$ between **A** (0, 0, 0) and **B** (3, 2, 1). (7 marks)